

General Relativity

Institute of Physics Bhubaneswar

Homework 4

Textbook: Sean Carroll's *Spacetime and Geometry*

Remember each homework carries weight.

Late submissions will not be accepted.

1. Starting with the action

$$I = \frac{1}{2} \int_{\gamma} g_{\mu\nu}(x) \frac{dx^{\mu}}{d\tau} \frac{dx^{\nu}}{d\tau} d\tau \quad (0.1)$$

along the path γ , and considering infinitesimal variations of the path (keeping end points fixed)

$$x^{\mu} \rightarrow x^{\mu} + \delta x^{\mu}, \quad (0.2)$$

show that the class of curves extremising the action I are geodesics.

2. Chapter 3, exercise 8.
3. Chapter 3, exercise 12.
4. Read section 3.10 and arrive at the geodesic deviation equation (3.208). Show your calculations.